

# pomegranate

fast and flexible probabilistic modelling in python

Jacob Schreiber

Paul G. Allen School of Computer Science & Engineering  
University of Washington



jmschreiber91



@jmschrei



@jmschreiber91



# Acknowledgements



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# Overview

pomegranate is **more flexible** than other packages, **fast**, is **intuitive to use**, and can do it all **in parallel**



# pomegranate supports many models

**Probability Distributions**

**General Mixture Models**

**Hidden Markov Models**

**Naive Bayes / Bayes' Classifiers**

**Markov Chains**

**Bayesian Networks**

**k-means / kmeans++ / kmeans||**

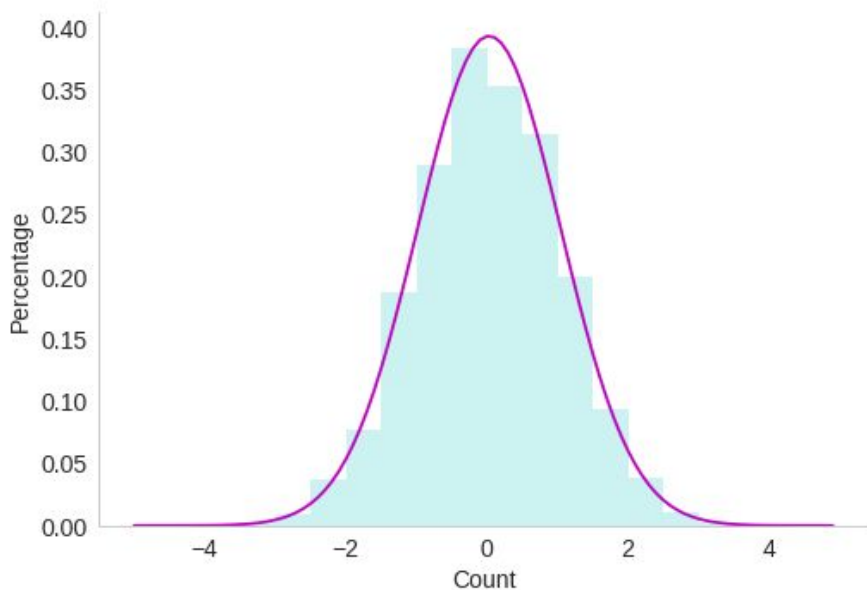
**Factor graphs**



# Models can be made in two ways...

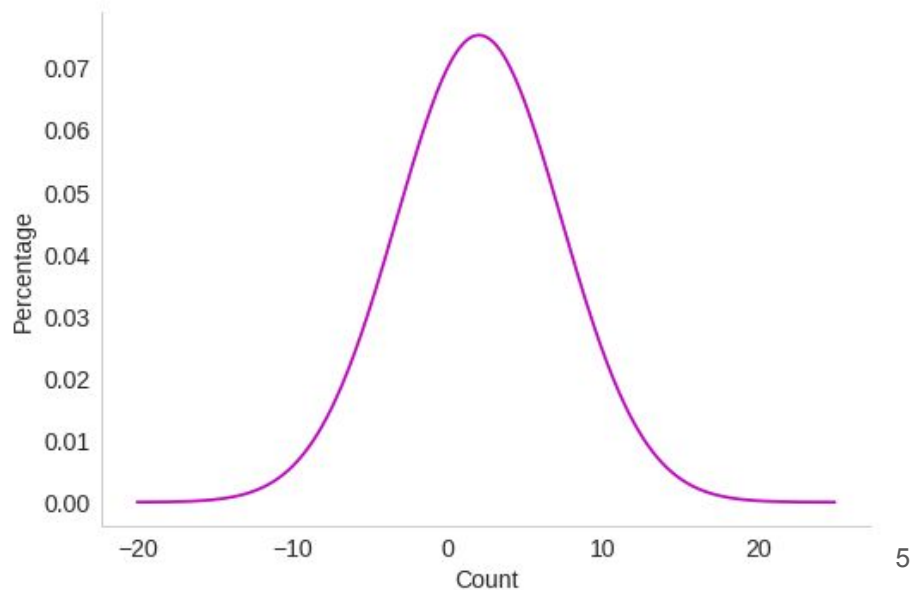
...from data

```
d = NormalDistribution.from_samples(X)
```



...from known values

```
d = NormalDistribution(5, 2.3)
```

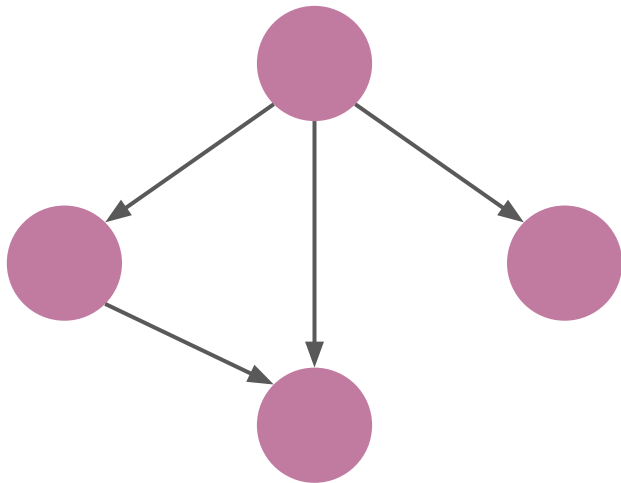




# Models can be made in two ways...

...from data

```
d = BayesianNetwork.from_samples(X)
```



...from known values

```
n1 = Node(...)  
n2 = Node(...)  
model = BayesianNetwork()  
model.add_nodes(n1, n2...)  
model.add_edges(...)
```



# The API is common to all models

`model.log_probability(X) / model.probability(X)`

`model.sample()`

`model.fit(X, weights, inertia)`

All models have these methods!

`model.summarize(X, weights)`

`model.from_summaries(inertia)`

`Model.from_samples(X, weights)`

`model.predict(X)`

`model.predict_proba(X)`

`model.predict_log_proba(X)`

All models composed of distributions (like GMM, HMM...) have these methods too!



# Overview: model stacking in pomegranate

```
GeneralMixtureModel.from_samples(NormalDistribution, n_components=3, X=X)
```

```
GeneralMixtureModel.from_samples(ExponentialDistribution, n_components=3,  
X=X)
```

```
BayesClassifier.from_samples(MultivariateGaussianDistribution, X, y)
```

```
d1 = GeneralMixtureModel.from_samples...
```

```
d2 = GeneralMixtureModel.from_samples...
```

```
model = BayesClassifier([d1, d2])
```





# pomegranate can be faster than numpy

Fitting Multivariate Gaussian to 10,000,000 samples of 10 dimensions

```
data = numpy.random.randn(10000000, 10)

print "numpy time:"
%timeit -n 10 data.mean(axis=0), numpy.cov(data, rowvar=False, bias=True)
print "\n" "pomegranate time:"
%timeit -n 10 MultivariateGaussianDistribution.from_samples(data)
```

numpy time:  
10 loops, best of 3: 3.52 s per loop

pomegranate time:  
10 loops, best of 3: 2.87 s per loop



# pomegranate uses additive summarization

pomegranate reduces data to sufficient statistics for updates and so only has to go datasets once (for all models).

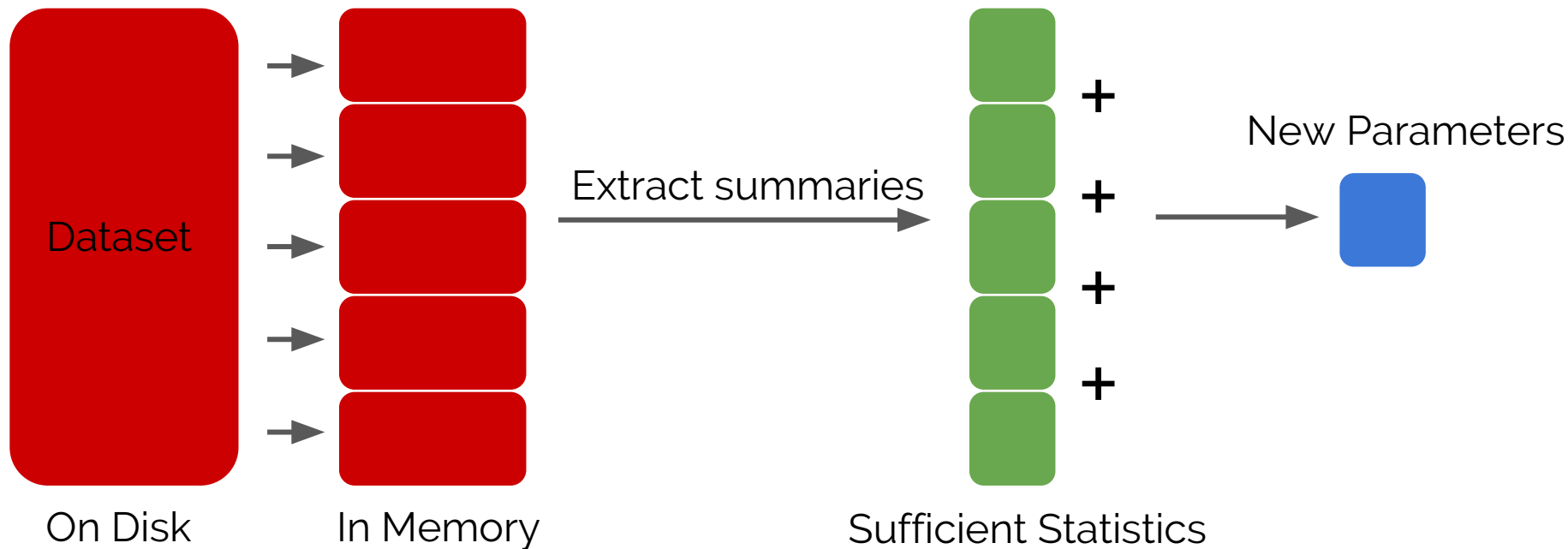
Here is an example of the Normal Distribution sufficient statistics

$$\sum_{i=1}^n w_i \quad \sum_{i=1}^n w_i x_i \quad \sum_{i=1}^n w_i x_i^2 \quad \longrightarrow \quad \begin{aligned} \mu &= \frac{\sum_{i=1}^n w_i x_i}{\sum_{i=1}^n w_i} \\ \sigma^2 &= \frac{\sum_{i=1}^n w_i x_i^2}{\sum_{i=1}^n w_i} - \frac{\left( \sum_{i=1}^n w_i x_i \right)^2}{\left( \sum_{i=1}^n w_i \right)^2} \end{aligned}$$



# pomegranate supports out-of-core learning

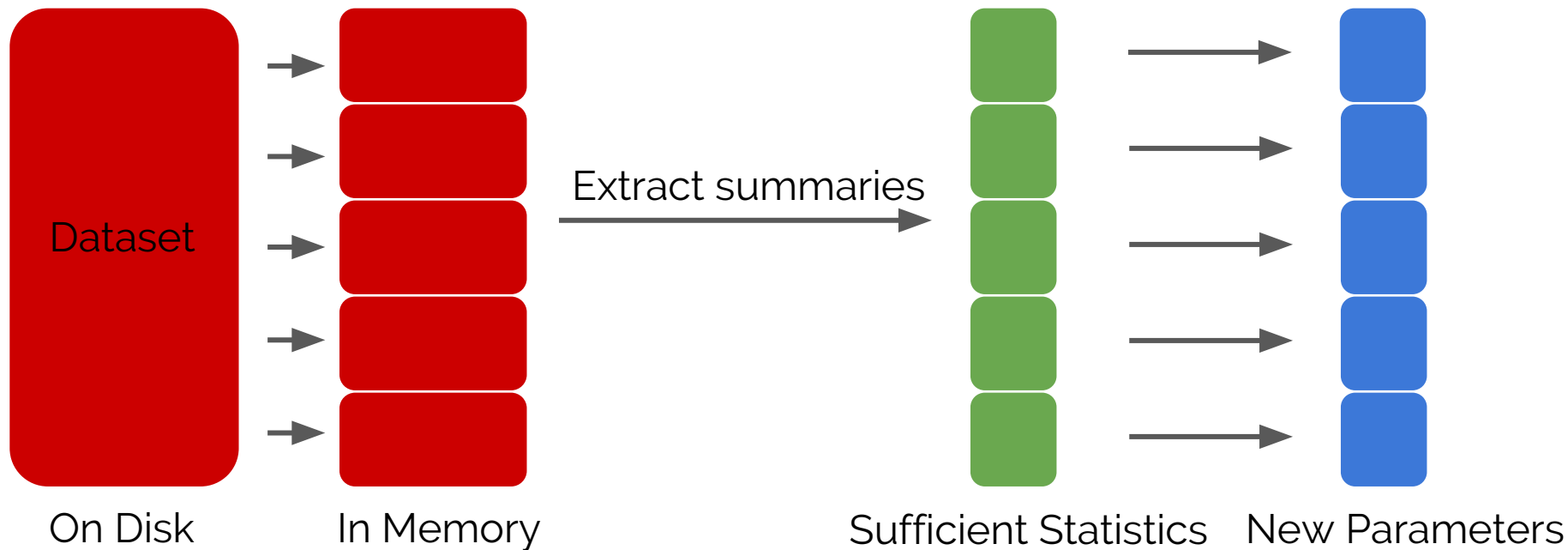
Batches from a dataset can be reduced to additive summary statistics, enabling exact updates from data that can't fit in memory.





# pomegranate supports mini-batching

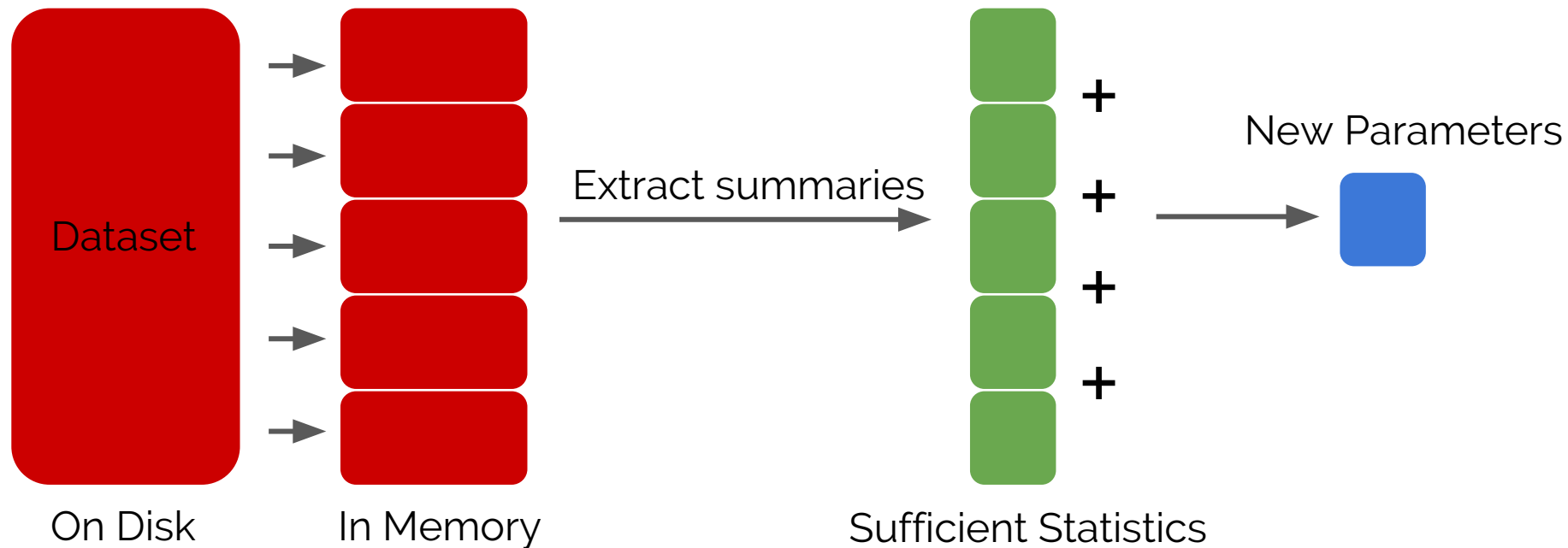
Instead of going through the full dataset before updating parameters, one could update parameters at each step.





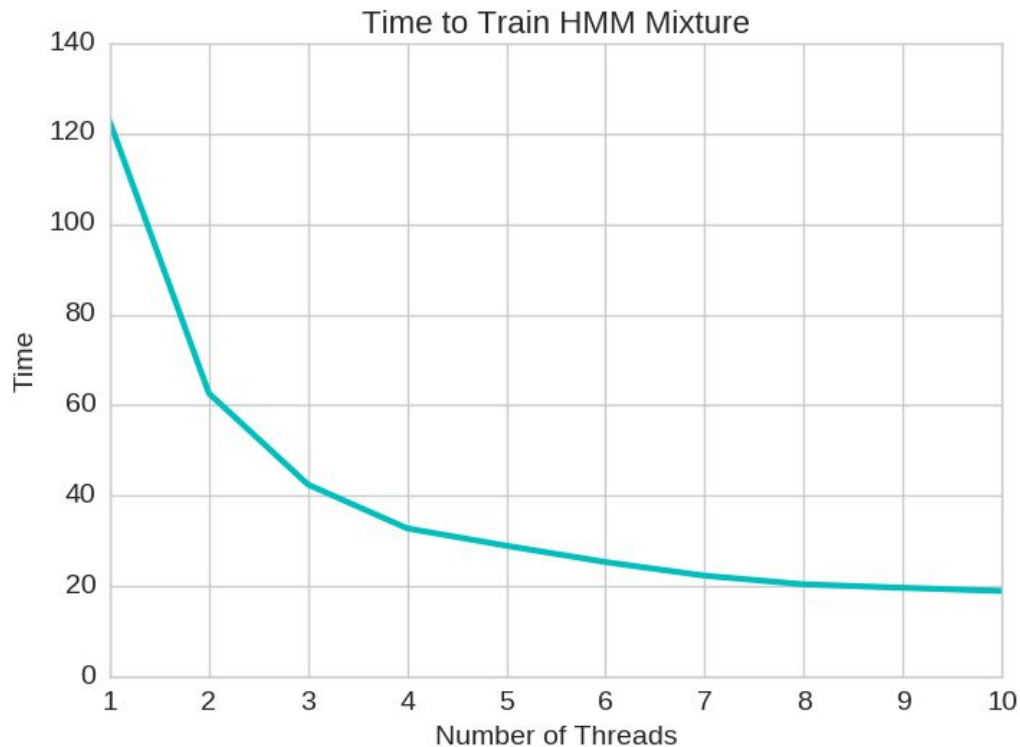
# pomegranate supports parallelization

Multiple batches can be loaded at the same time and processed by different threads using `n_jobs` in either fitting or prediction methods





# Training a mixture of HMMs in parallel

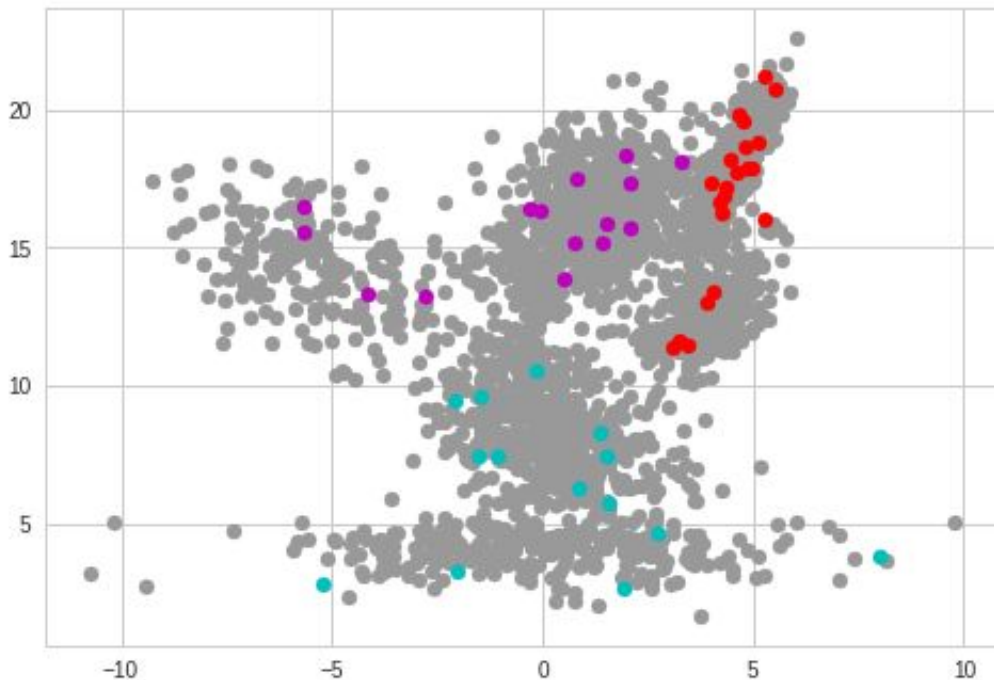


`model.fit(X, n_jobs=n)`



# pomegranate allows semisupervised learning

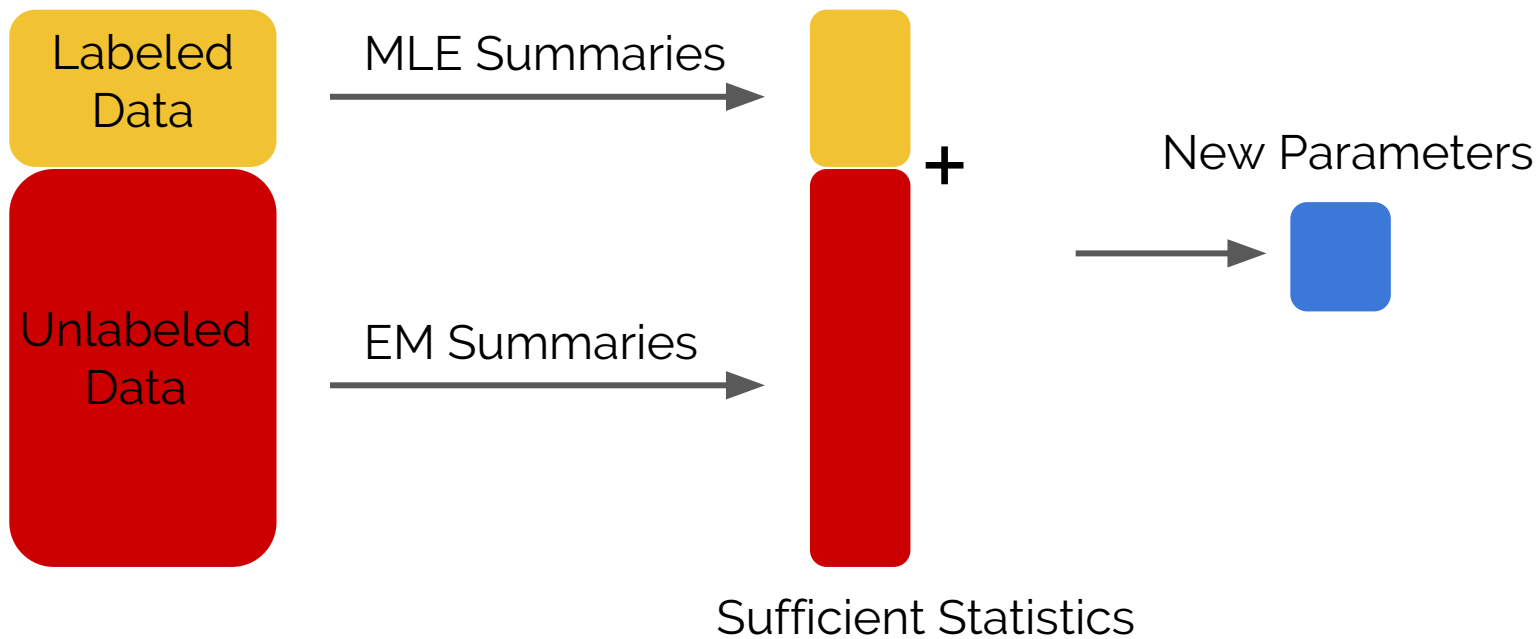
For many tasks, there is limited labeled data but a deluge of unlabeled data, and one wants to utilize both.





# pomegranate allows semisupervised learning

Summaries from MLE on the labeled data can be added to summaries from EM on the unlabeled data

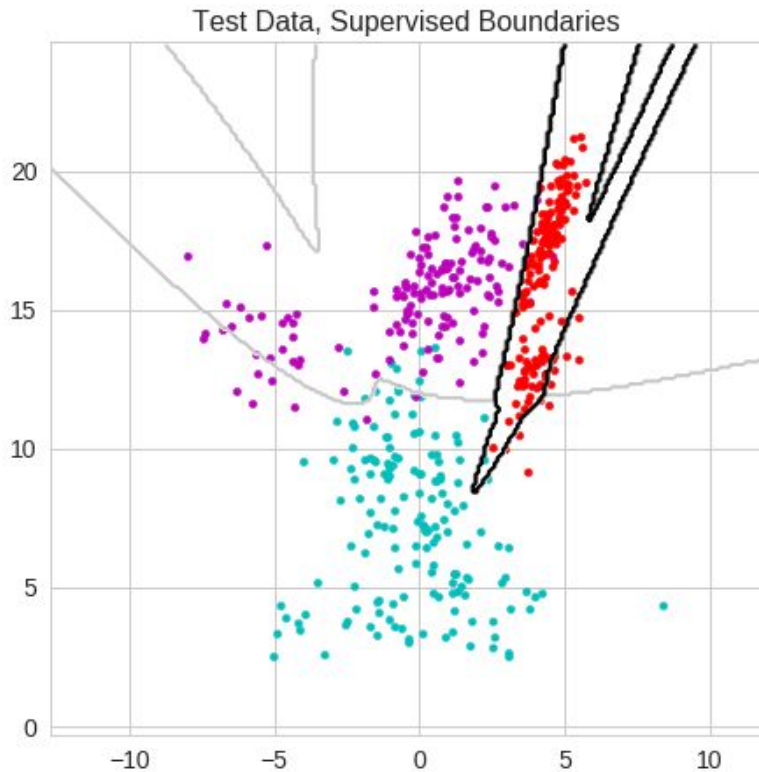




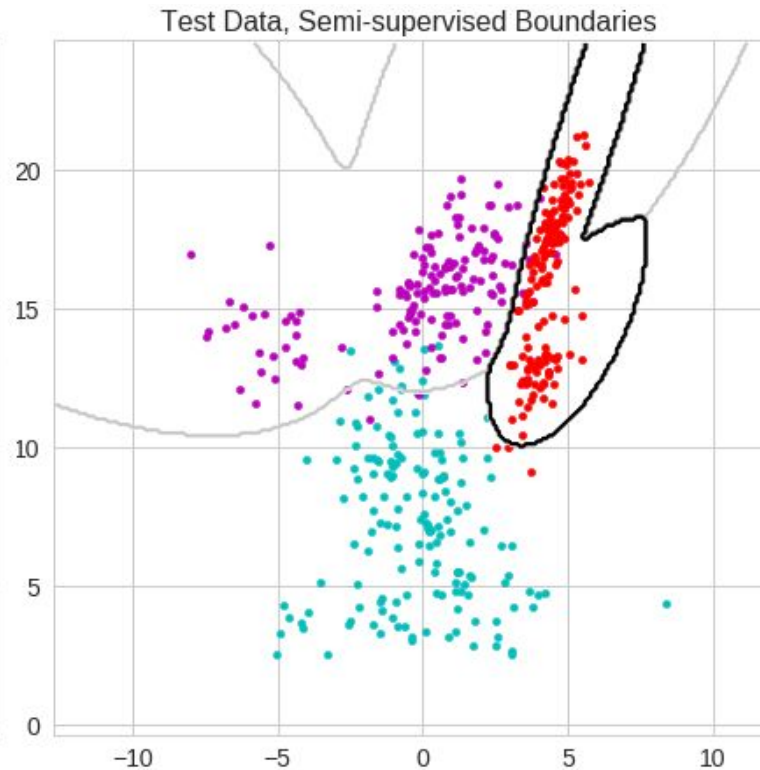


# pomegranate allows semisupervised learning

Supervised Accuracy: 0.93



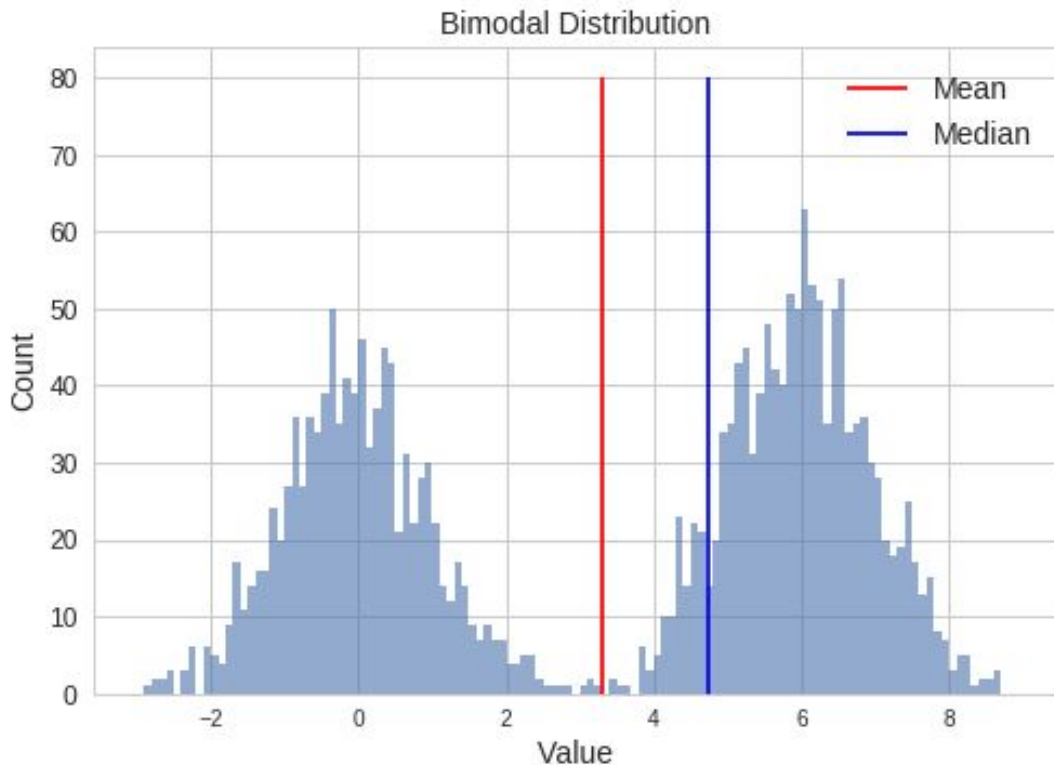
Semisupervised Accuracy: 0.96





# pomegranate supports missing data

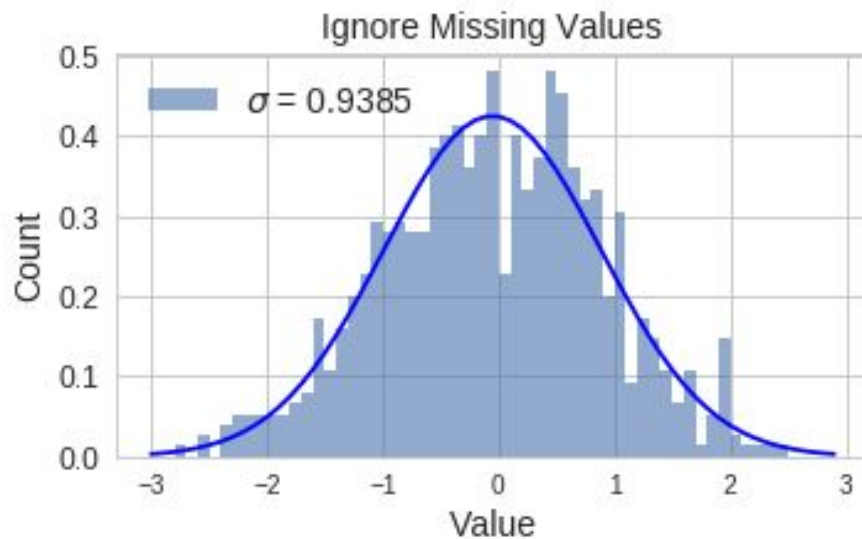
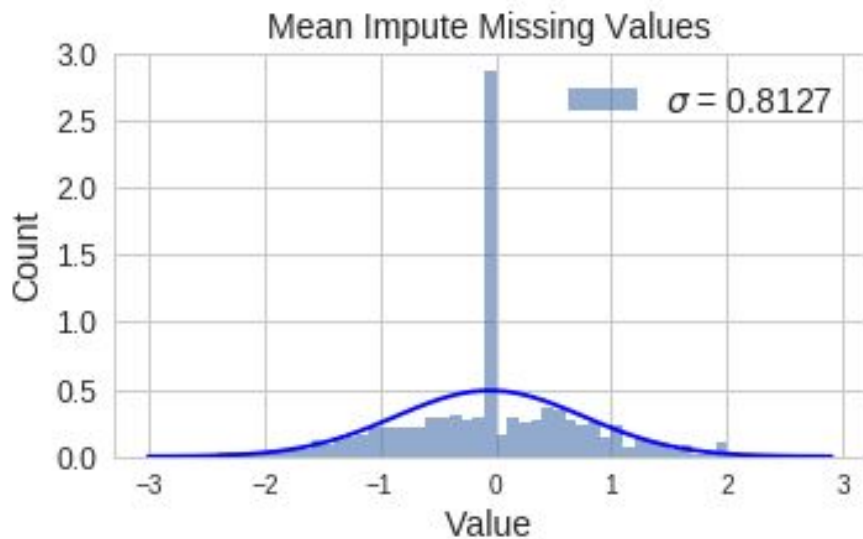
Many real world tasks involve missing data, but common approaches aren't sufficient for tackling the problem.





# pomegranate supports missing data

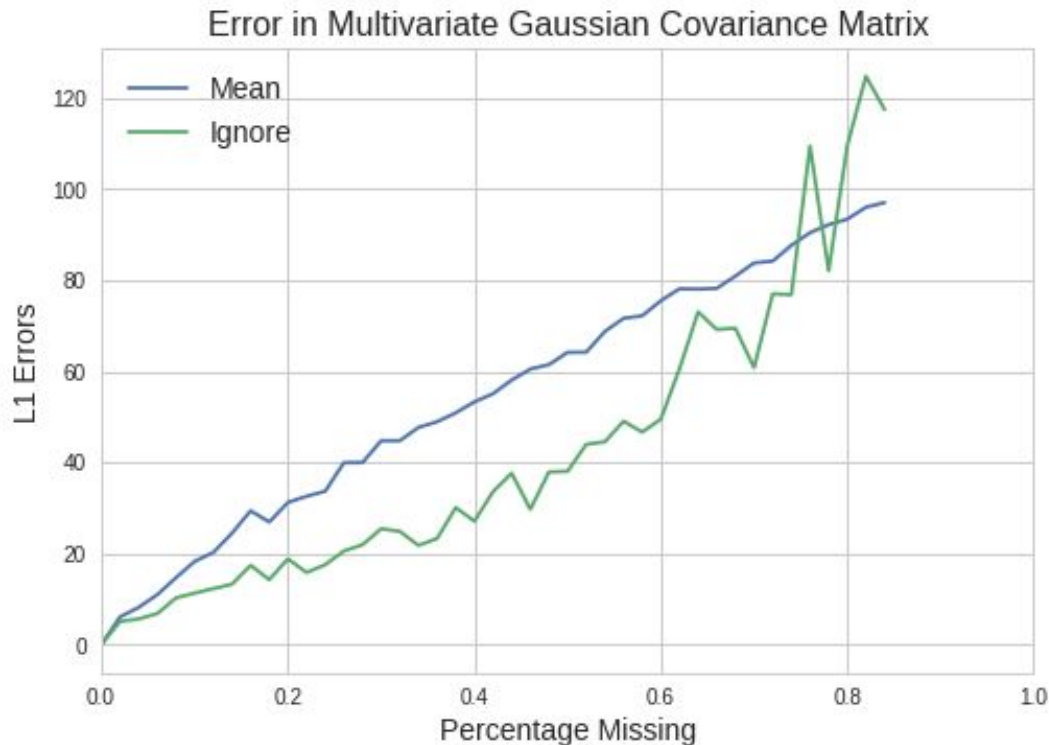
Many real world tasks involve missing data, but common approaches aren't sufficient for tackling the problem.





# pomegranate supports missing data

Many real world tasks involve missing data, but common approaches aren't sufficient for tackling the problem.





# pomegranate supports missing data

Pomegranate supports **model fitting**, **structure learning**, and **model predictions** on data sets that include missing values, no matter how complicated the model or sparse the data set.

You can **fit a Gaussian mixture model** to incomplete data sets.

You can run the **Viterbi or forward-backward algorithm** using a HMM on incomplete data sets.

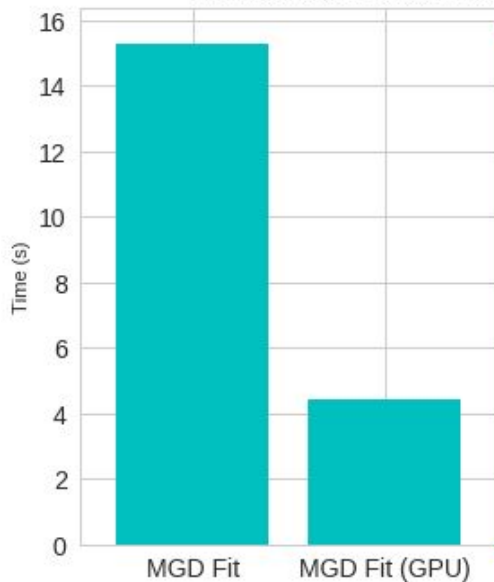
You can **learn the structure of a Bayesian network** on incomplete data sets.

All without having to change your command, simply by including `np.nan` in the place of the missing value



# pomegranate uses Cupy for GPU support

Multivariate Gaussian with GPU Acceleration





# pomegranate can be faster than scipy

```
mu, cov = numpy.random.randn(2000), numpy.eye(2000)
d = MultivariateGaussianDistribution(mu, cov)
X = numpy.random.randn(2000, 2000)
print "scipy time: ",
%timeit multivariate_normal.logpdf(X, mu, cov)
print "pomegranate time: ",
%timeit MultivariateGaussianDistribution(mu, cov).log_probability(X)
print "pomegranate time (w/ precreated object): ",
%timeit d.log_probability(X)
```

```
scipy time: 1 loop, best of 3: 1.67 s per loop
pomegranate time: 1 loop, best of 3: 801 ms per loop
pomegranate time (w/ precreated object): 1 loop, best of 3: 216 ms per loop
```



# pomegranate uses aggressive caching

$$P(X|\mu, \sigma) = \frac{1}{\sqrt{2\pi}\sigma} \exp \left( -\frac{(x - \mu)^2}{2\sigma^2} \right)$$

$$\log P(X|\mu, \sigma) = -\log(\sqrt{2\pi}\sigma) - \frac{(x - \mu)^2}{2\sigma^2}$$

$$\log P(X|\mu, \sigma) = \alpha - \frac{(x - \mu)^2}{\beta}$$





# GOSSIP GIRL



## Example 'blast' from Gossip Girl

Spotted: Lonely Boy. Can't believe the love of his life has returned. If only she knew who he was. But everyone knows Serena. And everyone is talking. Wonder what Blair Waldorf thinks. Sure, they're BFF's, but we always thought Blair's boyfriend Nate had a thing for Serena.



## Example 'blast' from Gossip Girl

Why'd she leave? Why'd she return? Send me all the deets.  
And who am I? That's the secret I'll never tell. The only one.  
—XOXO. Gossip Girl.



# How do we encode these 'blasts'?

Better lock it down with Nate, B. Clock's ticking.

+1 Nate

-1 Blair



# How do we encode these 'blasts'?

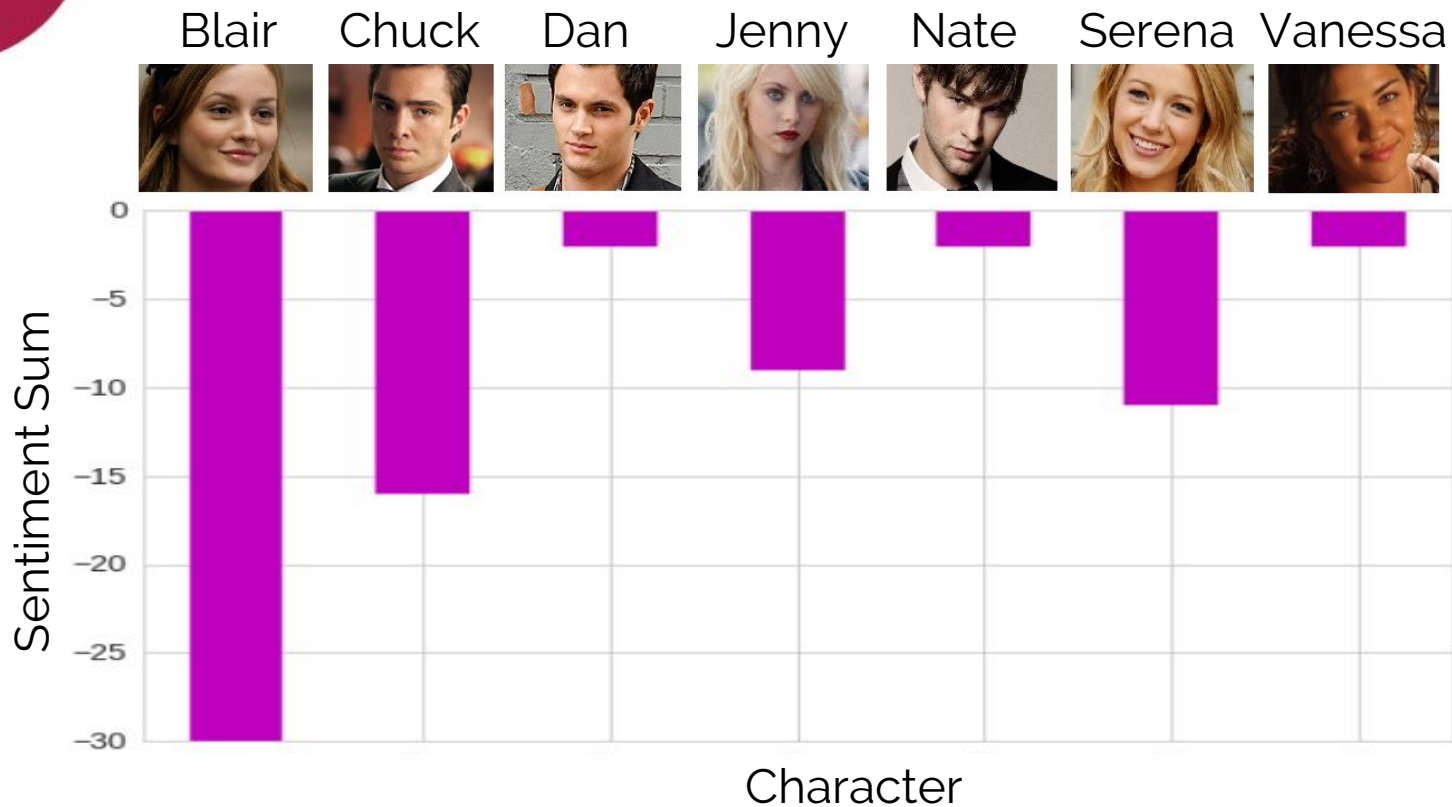
This just in: S and B committing a crime of fashion. Who doesn't love a five-finger discount. Especially if it's the middle one.

-1 Blair

-1 Serena

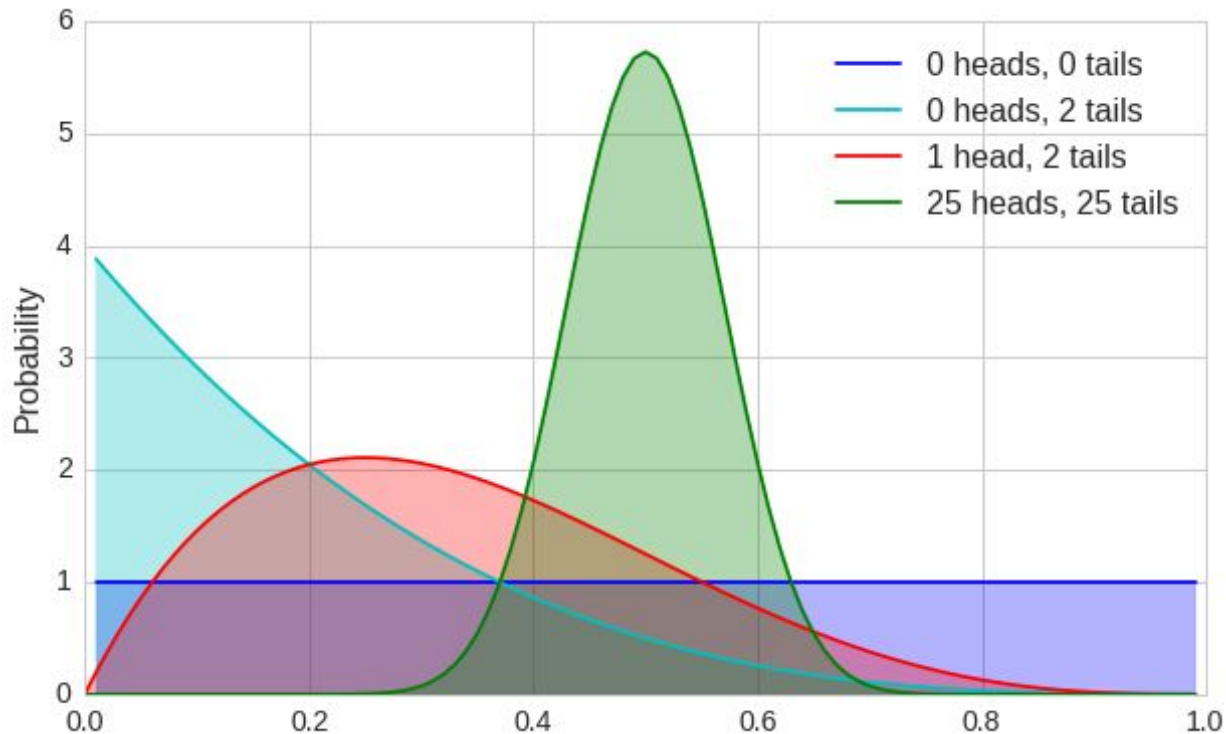


# Simple summations don't work well



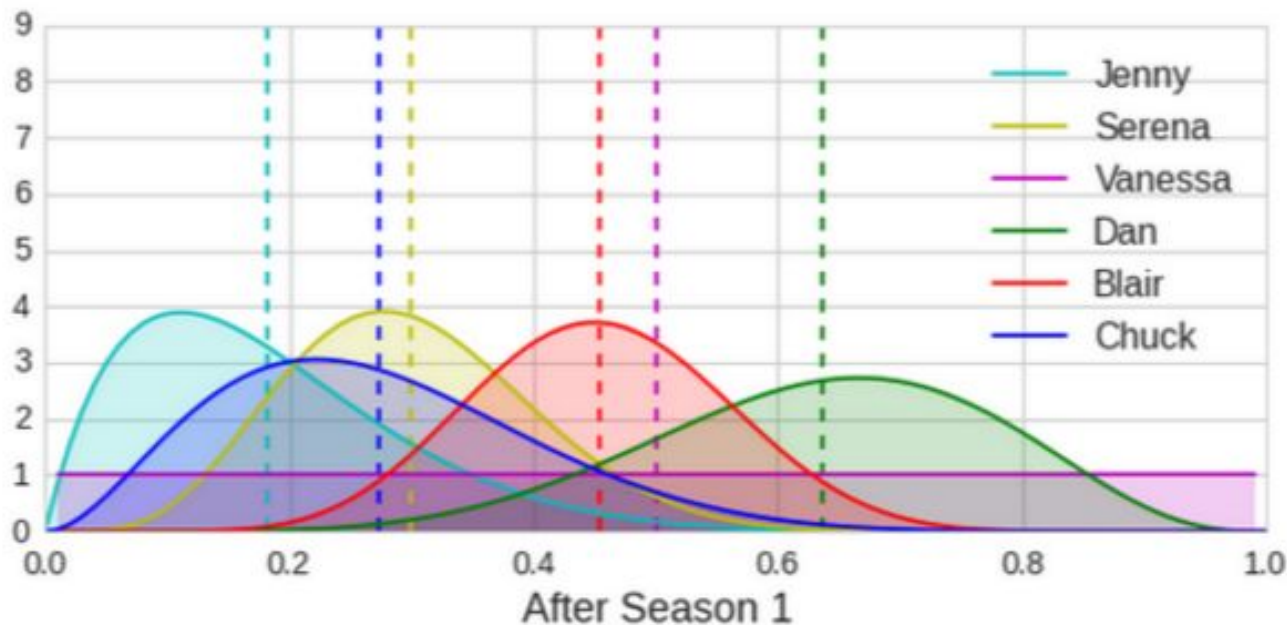


# Beta distributions can model uncertainty





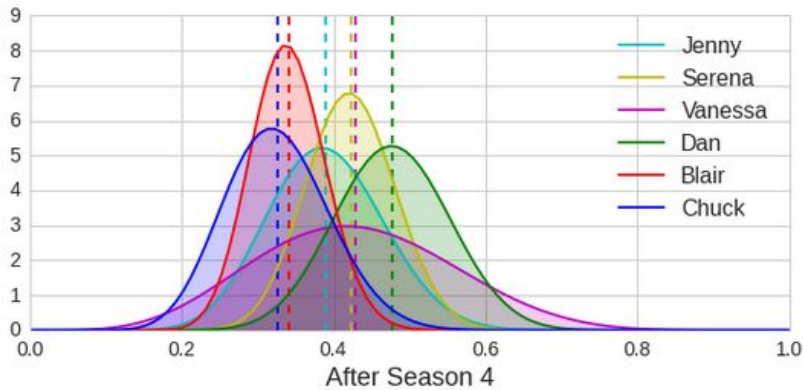
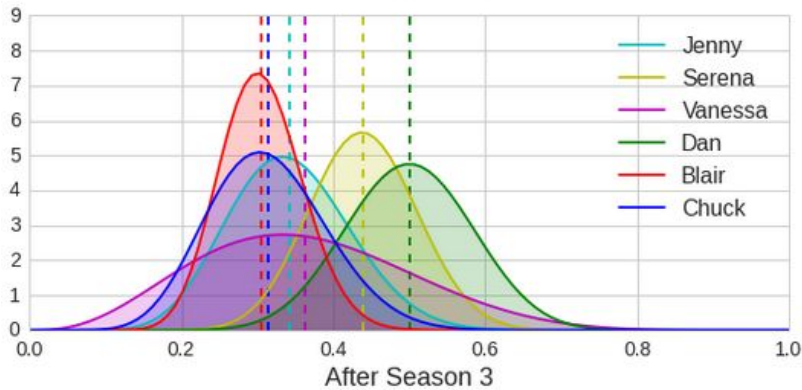
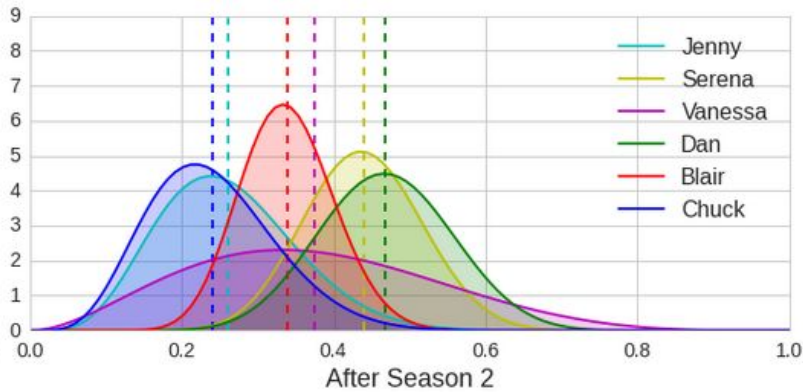
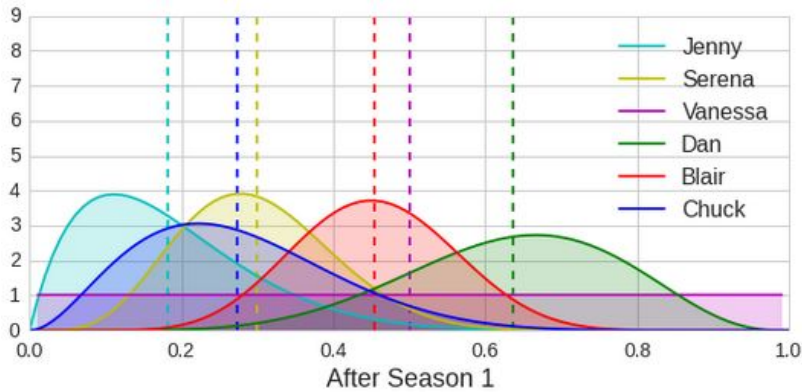
# Beta distributions can model uncertainty







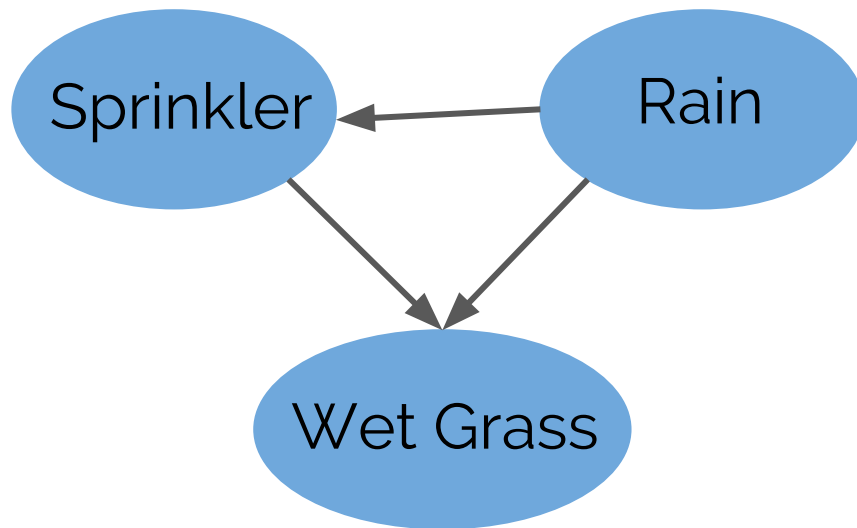
# Beta distributions can model uncertainty





# Bayesian networks

Bayesian networks are powerful inference tools which define a dependency structure between variables.

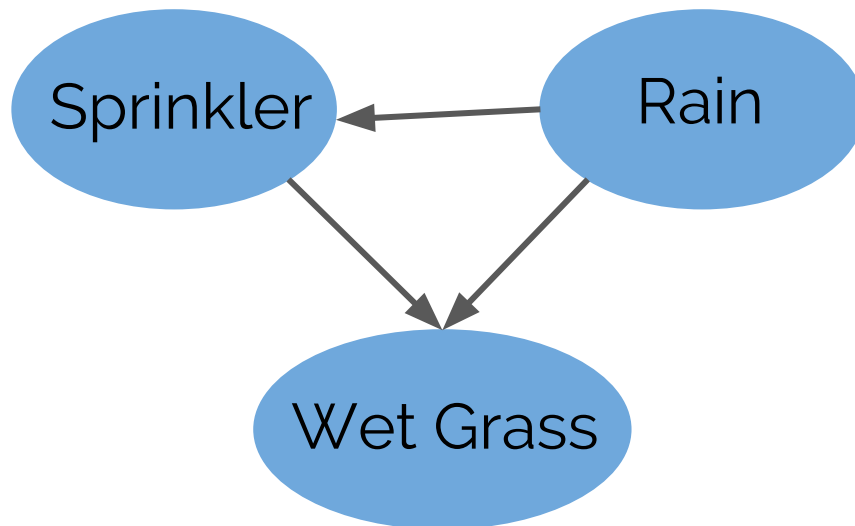




# Bayesian networks

Two main difficult tasks:

- (1) Inference given incomplete information
- (2) Learning the dependency structure from data





# Bayesian network structure learning

???

Three primary ways:

- “Search and score” / Exact
- “Constraint Learning” / PC
- Heuristics



# Bayesian network structure learning

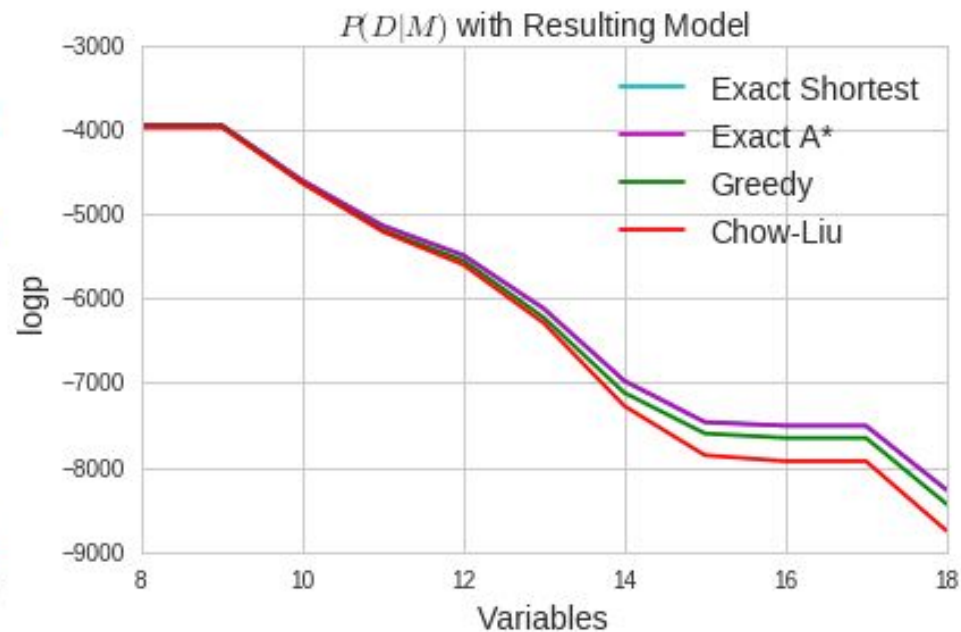
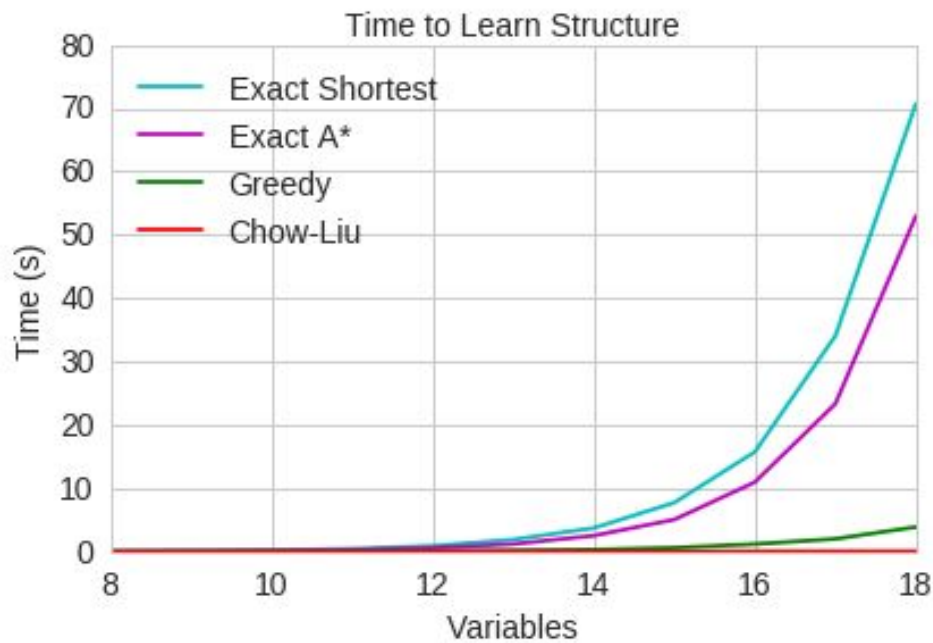
???

pomegranate supports:

- “Search and score” / Exact
- “Constraint Learning” / PC
- Heuristics



# pomegranate supports four algorithms





# BNSL is hard due to acyclicity requirement

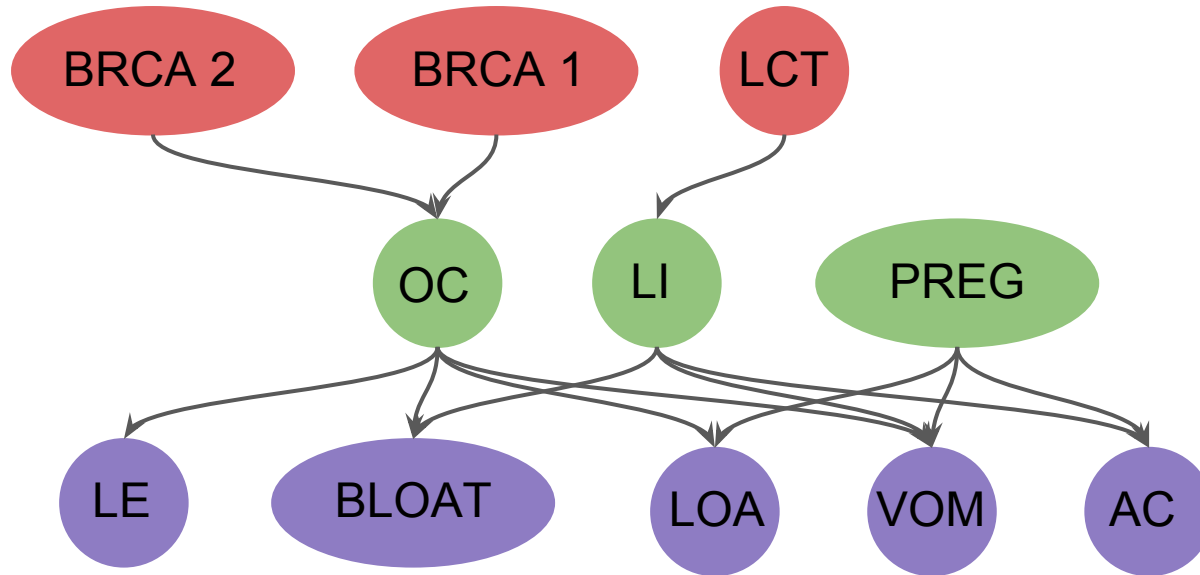
Easy! Tractable!

**Global Parameter Independence:** The parents of some variable  $A$  are independent of the parents of some variable  $B$  given that they don't form a cycle in the resulting graph

Hard! Exponential Time!



# Medical diagnosis Bayesian network

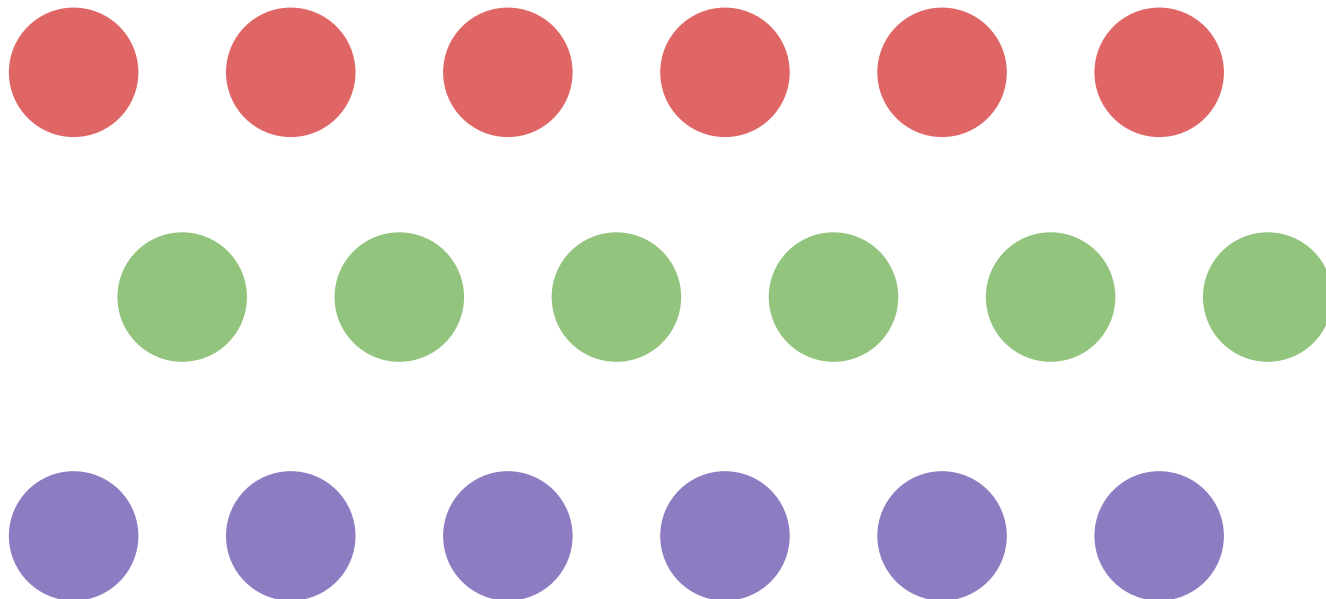




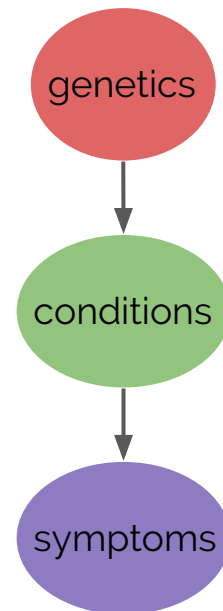


# Constraint graphs merge data + knowledge

Variables to be Modeled



Constraint Graph

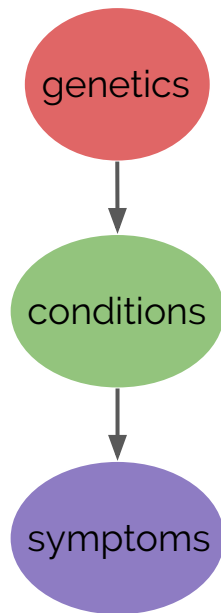




# Constraint graphs merge data + knowledge

**Global Parameter Independence:** The parents of some variable  $A$  are independent of the parents of some variable  $B$  given that they don't form a cycle in the resulting graph

Constraint Graph

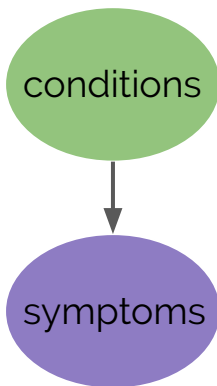




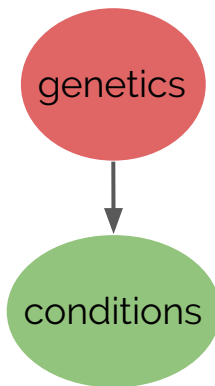
# Constraint graphs merge data + knowledge

The parents of some variable A are independent of the parents of some variable B

Task #1



Task #2

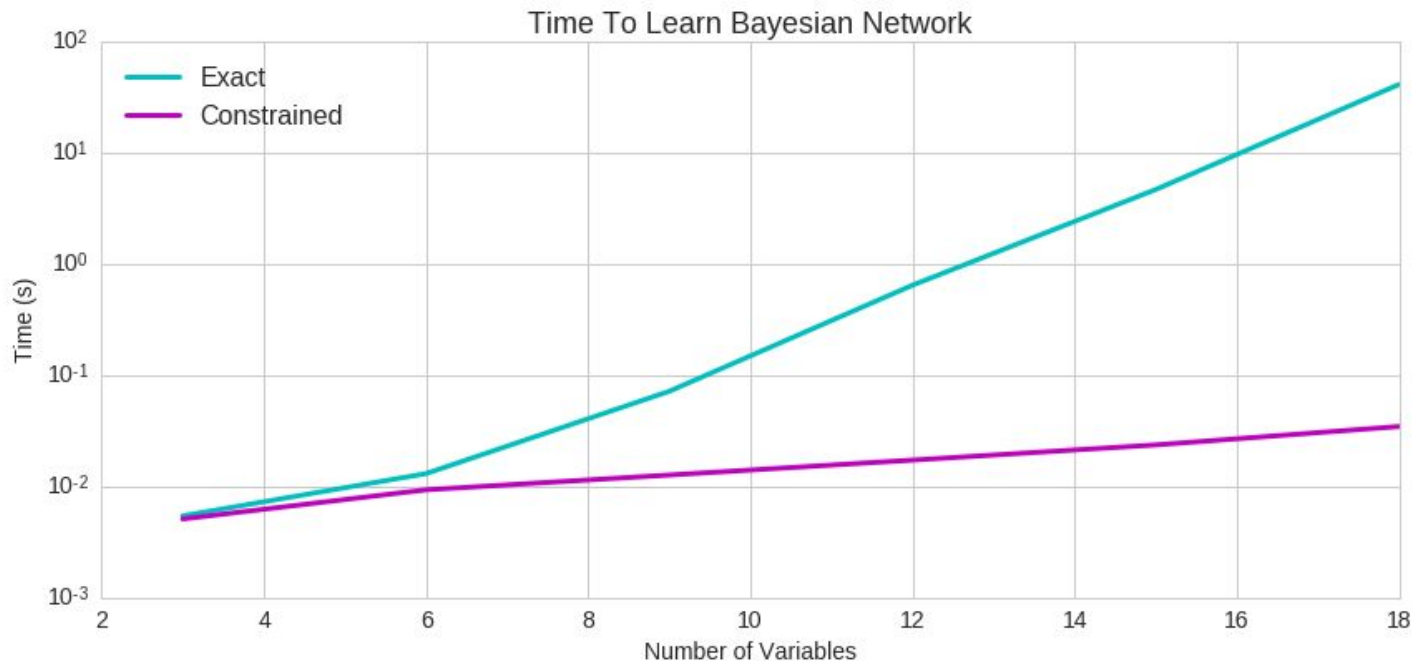


Task #3

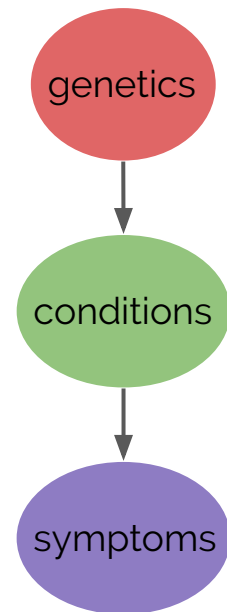




# Constraint graphs merge data + knowledge

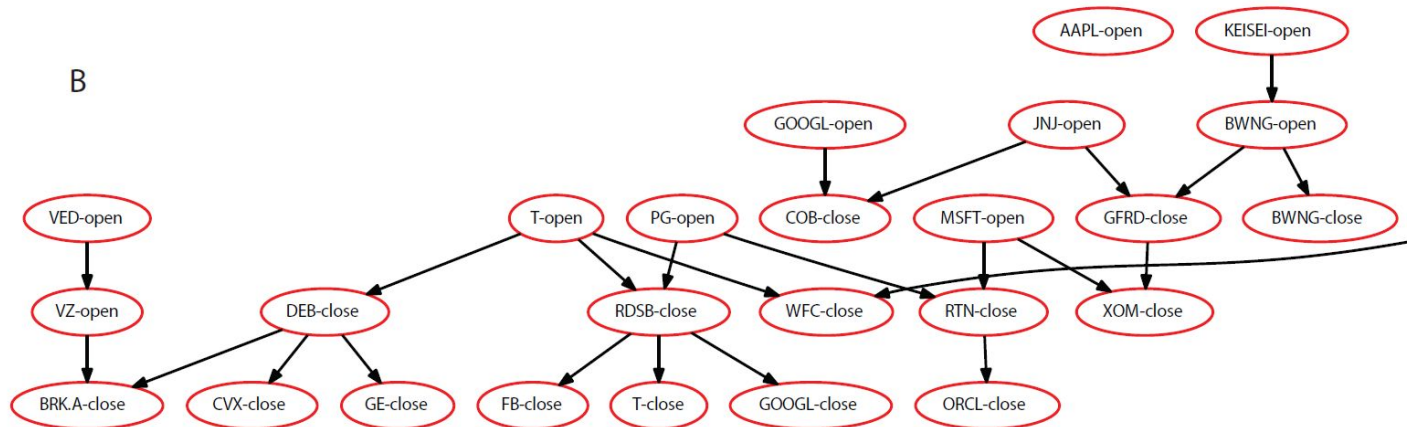
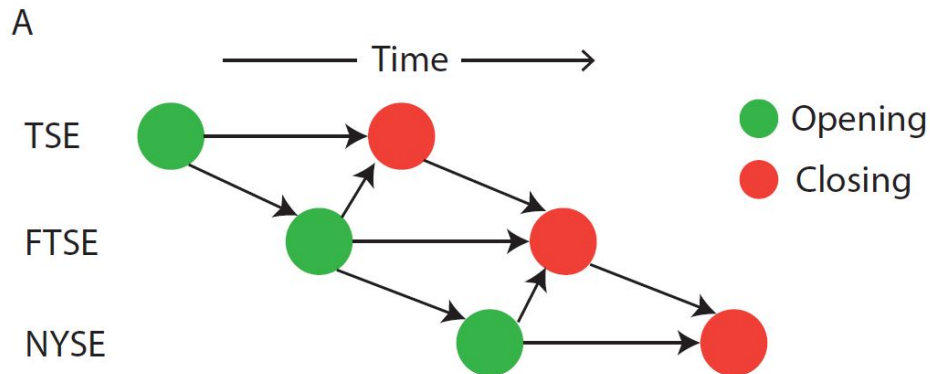


## Constraint Graph





# Modeling the global stock market





## Finding the optimal Bayesian network given a constraint graph

Jacob M. Schreiber<sup>1</sup> and William S. Noble<sup>2</sup>

<sup>1</sup>Department of Computer Science, University of Washington, Seattle, WA, United States of America

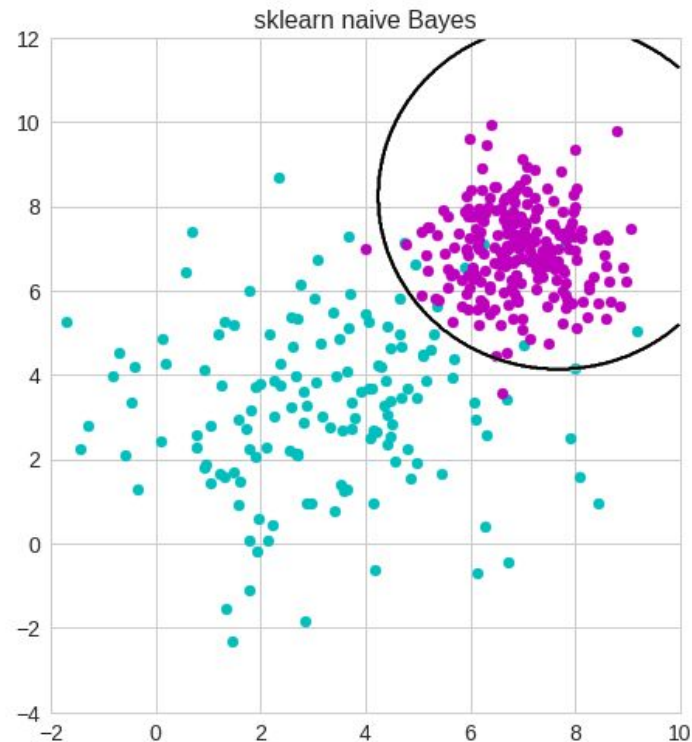
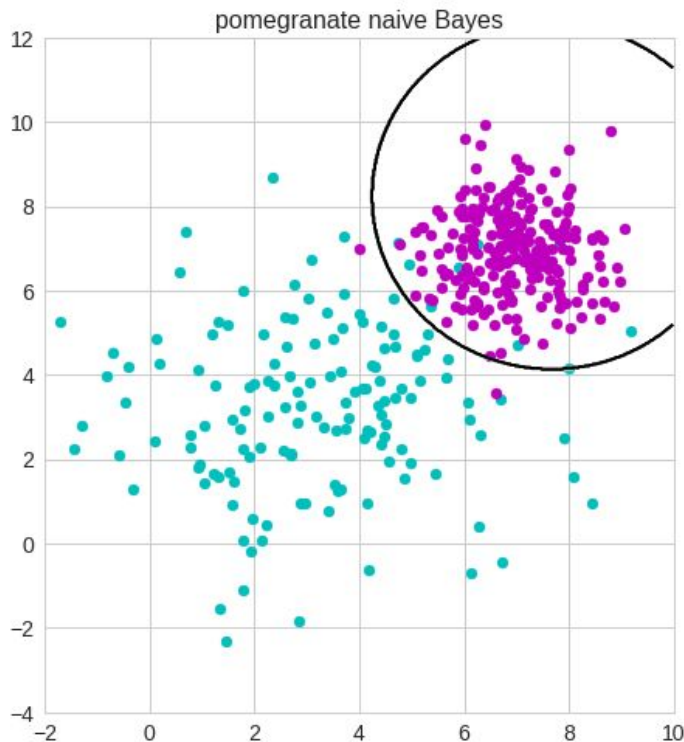
<sup>2</sup>Department of Genome Science, University of Washington, Seattle, WA, United States of America

### ABSTRACT

Despite recent algorithmic improvements, learning the optimal structure of a Bayesian network from data is typically infeasible past a few dozen variables. Fortunately, domain knowledge can frequently be exploited to achieve dramatic computational savings, and in many cases domain knowledge can even make structure learning tractable. Several methods have previously been described for representing this type of structural prior



# Naive Bayes produces ellipsoid boundaries



```
model = NaiveBayes.from_samples(NormalDistribution, X, y)
```



# Naive Bayes assumes independent features

$$\textit{Posterior} = \frac{\textit{Likelihood} * \textit{Prior}}{\textit{Normalization}}$$

$$P(M|D) = \frac{\prod_{i=1}^d P(D_i|M)P(M)}{\sum_M \prod_{i=1}^d P(D_i|M)P(M)}$$

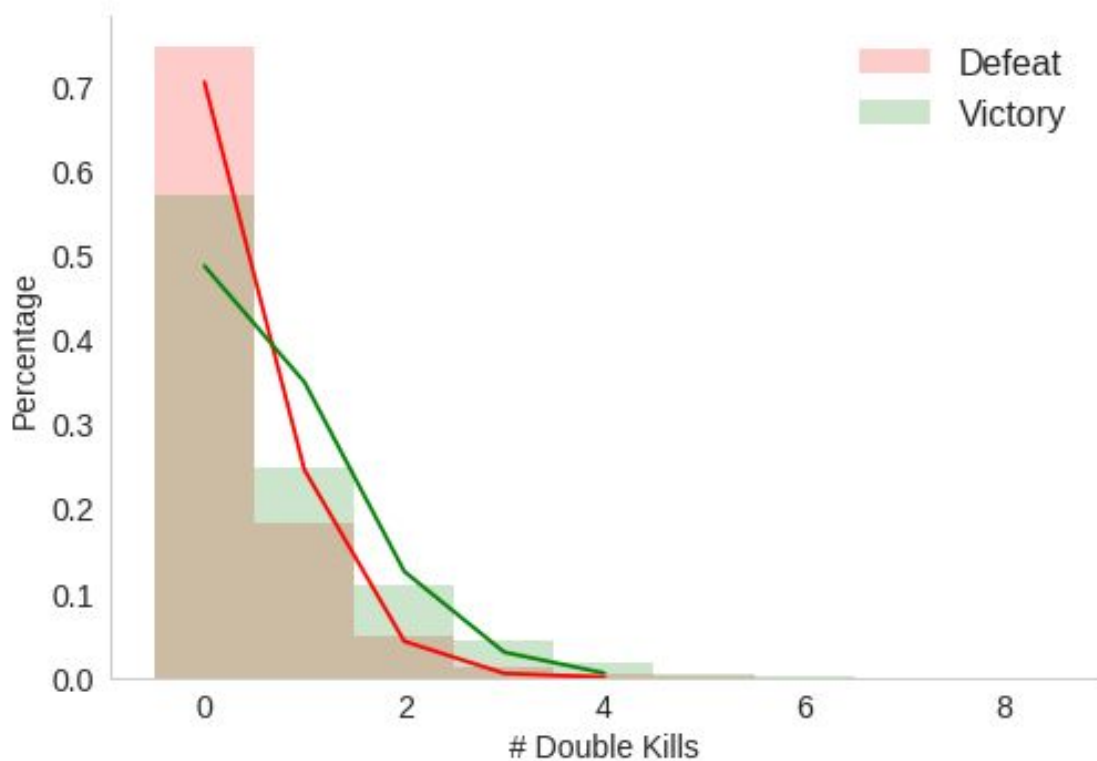


The background of the image is a detailed illustration of a fantasy landscape. In the foreground, there are dark, jagged rock formations and some green pine trees on the left. In the middle ground, there are several stone statues and ruins, some of which are glowing with a bright blue light. In the background, there are more ruins and a large, imposing structure that looks like a temple or a castle. The sky is a mix of orange, yellow, and blue, suggesting a sunset or sunrise. The overall style is that of a high-quality video game background.

# LEAGUE OF LEGENDS®

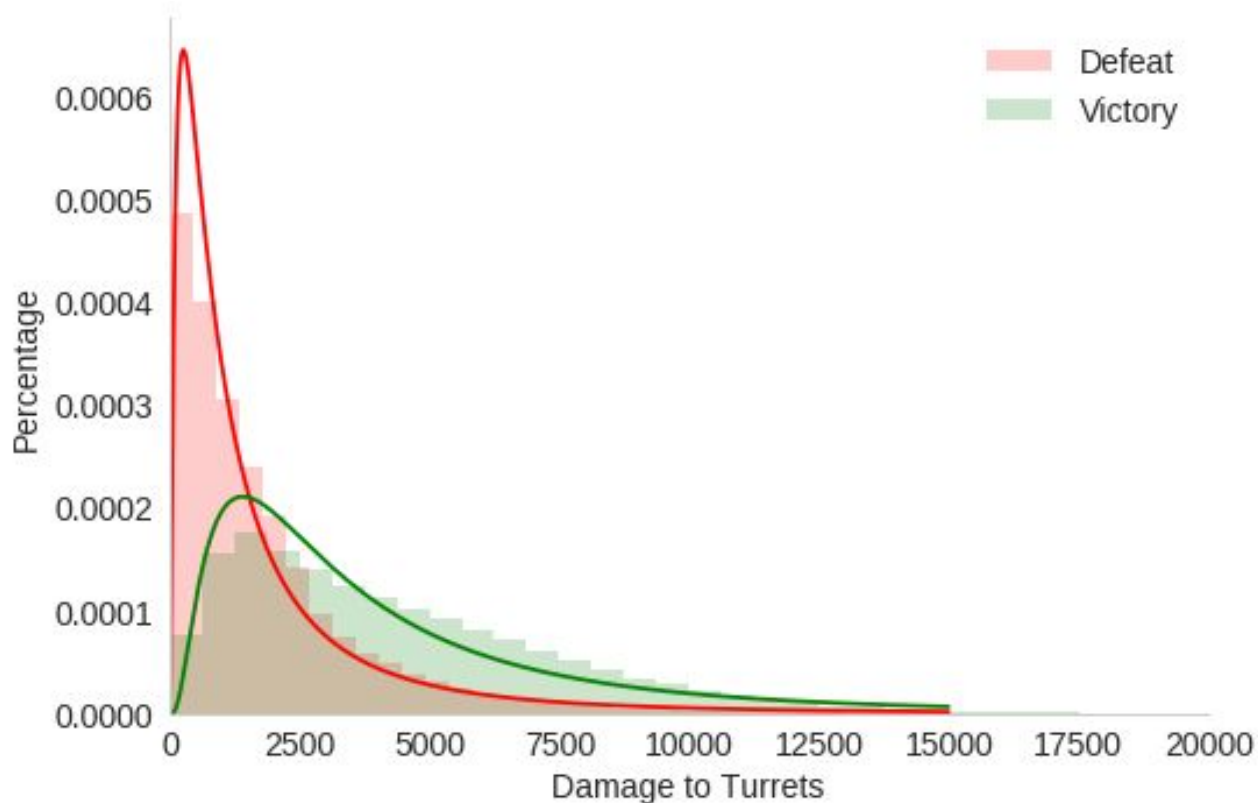


# Data can fall under different distributions



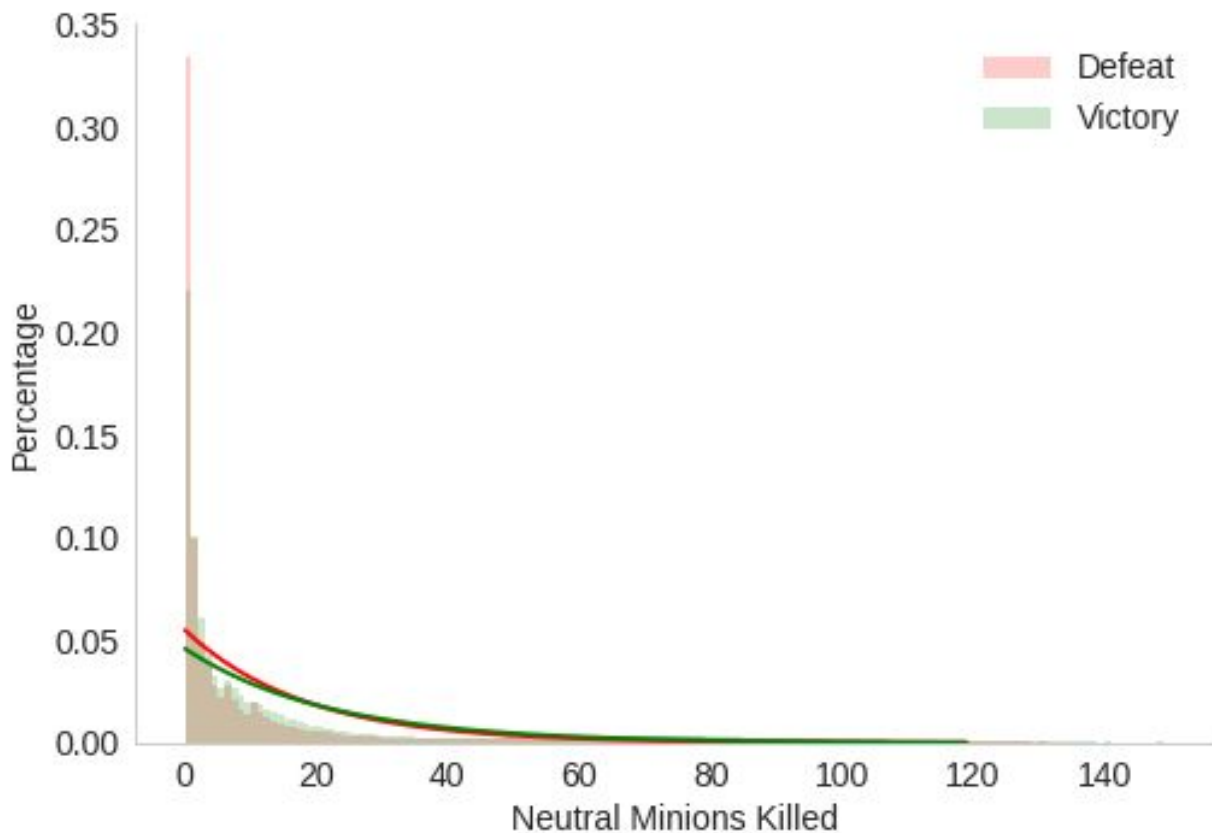


# Data can fall under different distributions





# Data can fall under different distributions





# Using appropriate distributions is best

```
dists = [LogNormalDistribution, PoissonDistribution,  
ExponentialDistribution, PoissonDistribution]
```

```
model1 = NaiveBayes.from_samples(NormalDistribution, X, y)  
model2 = NaiveBayes.from_samples(dists, X, y)  
model3 = GaussianNB().fit(X, y)
```

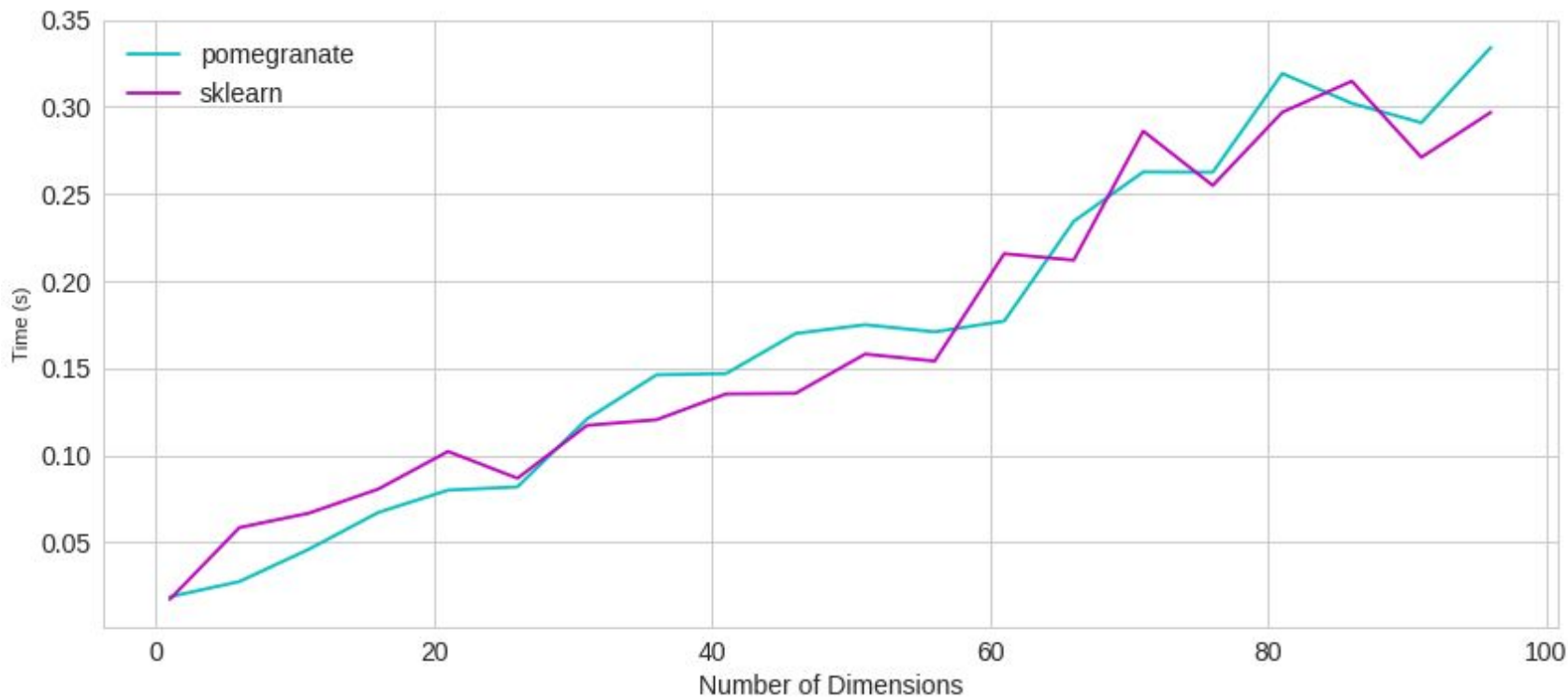
pomegranate Gaussian Naive Bayes: 0.711

sklearn Gaussian Naive Bayes: 0.711

Heterogeneous Naive Bayes: 0.726



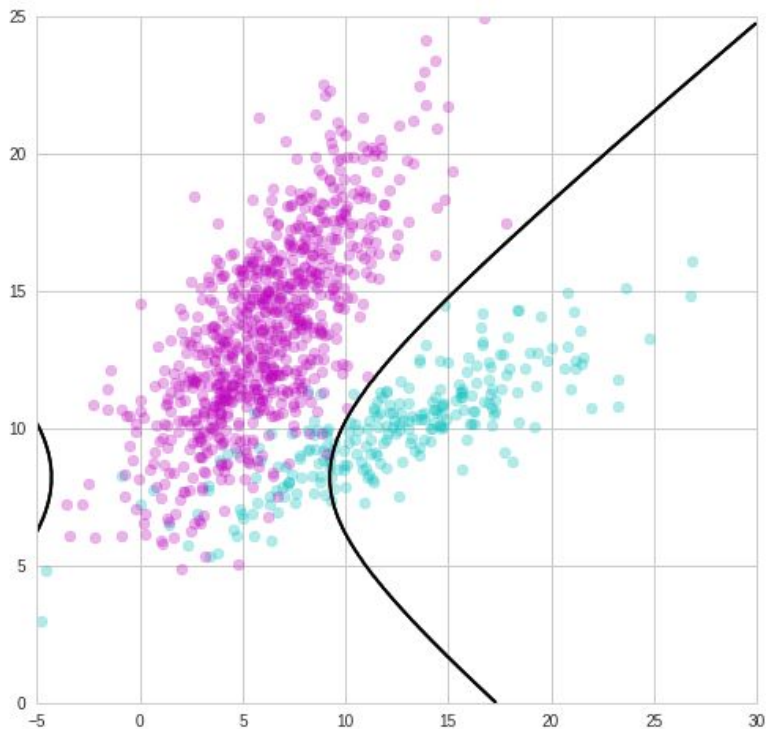
# This additional flexibility is just as fast



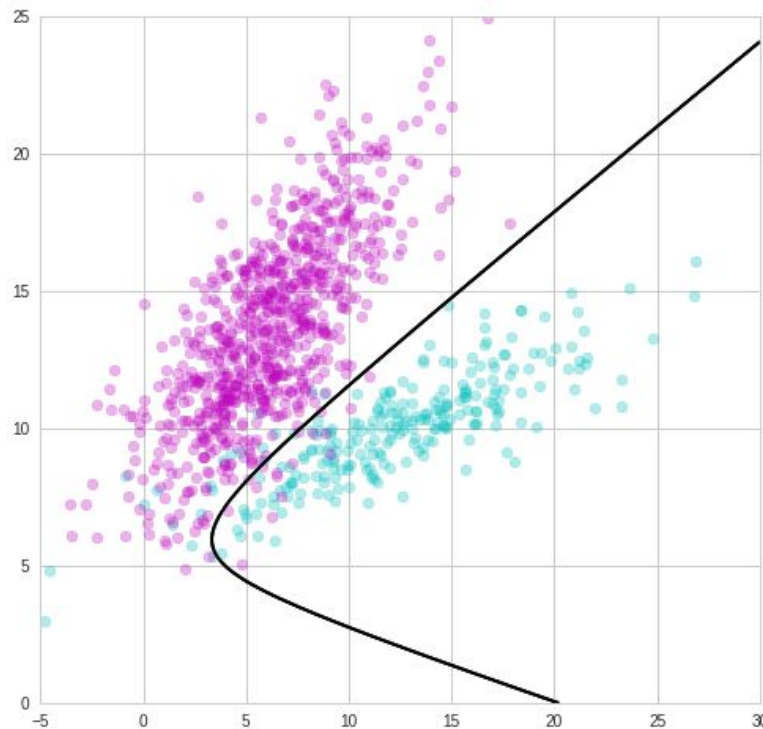


# Bayes classifiers don't require independence

naive accuracy: 0.929



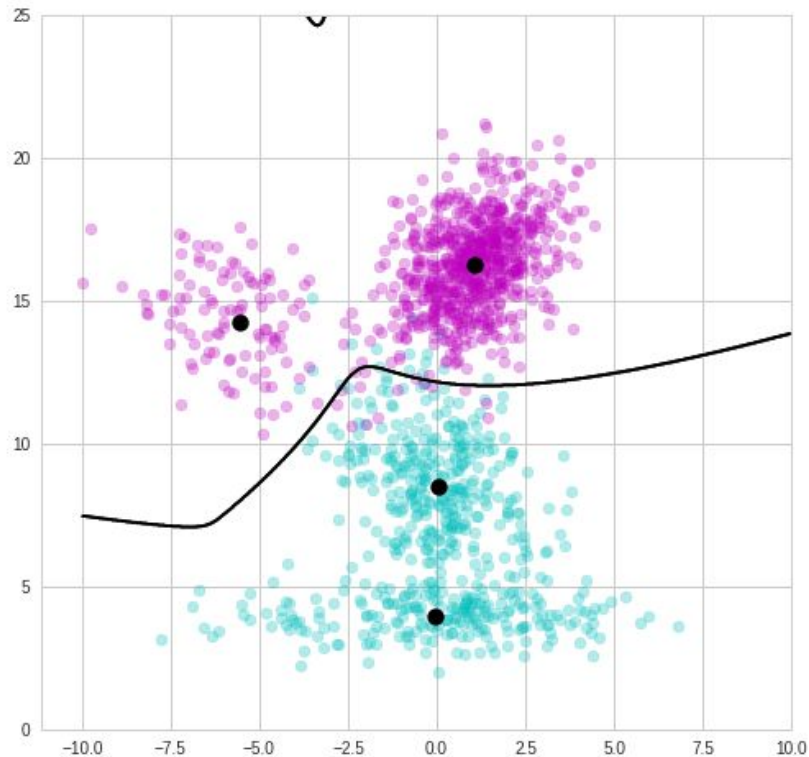
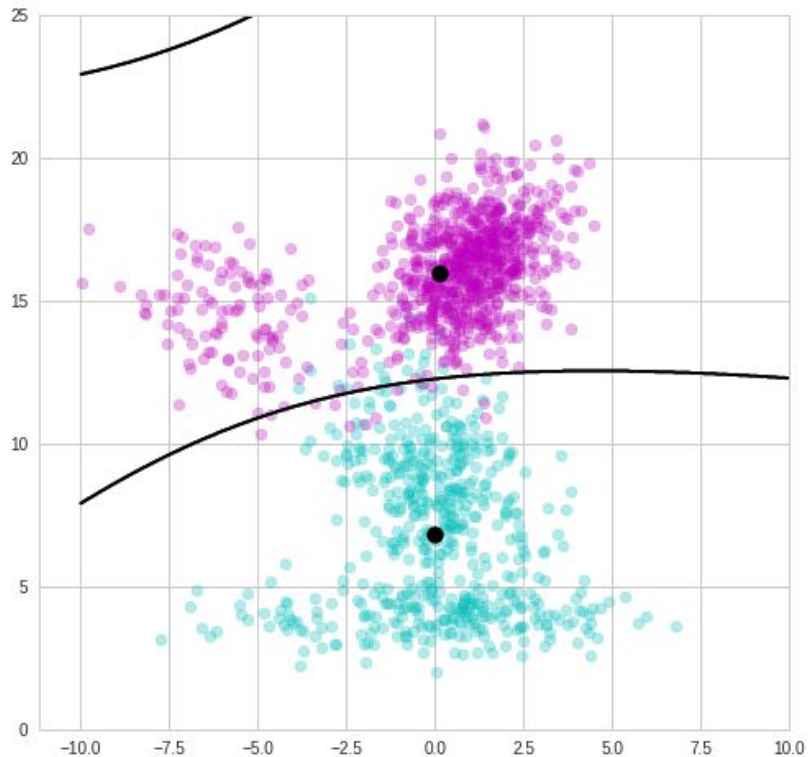
bayes classifier accuracy: 0.966







# Gaussian mixture model Bayes classifier







# pomegranate paper at JMLR-MLOSS

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## **pomegranate: fast and flexible probabilistic modeling in python**

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**Jacob Schreiber**

Paul G. Allen School of Computer Science  
University of Washington  
Seattle, WA 98195  
`jmschr@cs.washington.edu`

### **Abstract**

We present pomegranate, an open source machine learning package for probabilistic modeling in Python. Probabilistic modeling encompasses a wide range of methods that explicitly describe uncertainty using probability distributions. Three widely used probabilistic models implemented in pomegranate are general mixture models, hidden Markov models, and Bayesian networks. A primary focus of pomegranate is to abstract away the complexities of training models from their definition. This allows users to focus on specifying the correct model for their



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## pomegranate

pomegranate is a Python module for fast and flexible probabilistic modeling inspired by the design of scikit-learn. A primary focus of pomegranate is to abstract away the intricacies of a model from its definition, allowing users to easily prototype with complex models and training strategies. Its modular implementation allows for probability distributions to be swapped in or out for each other with ease and for models to be stacked within each other, yielding such delights as a mixture of Bayesian networks or a Gaussian mixture model Bayes classifier.

<https://www.numfocus.org/open-source-projects/affiliated-projects/>



# Documentation available at Readthedocs

 **pomegranate**  
latest

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build passing

 build passing

docs passing

## Home

pomegranate is a python package which implements fast, efficient, and extremely flexible probabilistic models ranging from probability distributions to Bayesian networks to mixtures of hidden Markov models. The most basic level of probabilistic modeling is the a simple probability distribution. If we're modeling language, this may be a simple distribution over the frequency of all possible words a person can say.
















### 1. [Probability Distributions](#)

The next level up are probabilistic models which use the simple distributions in more complex ways. A markov chain can extend a simple probability distribution to say that the probability of a certain word depends on the word(s) which have been said previously. A hidden Markov model may say that the probability of a certain words depends on the latent/hidden state of the previous word,

<https://pomegranate.readthedocs.io/en/latest/>

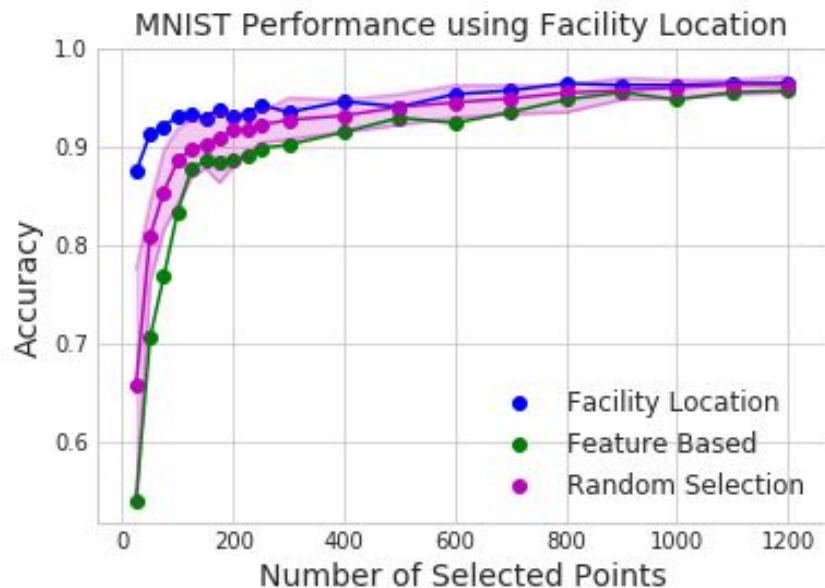
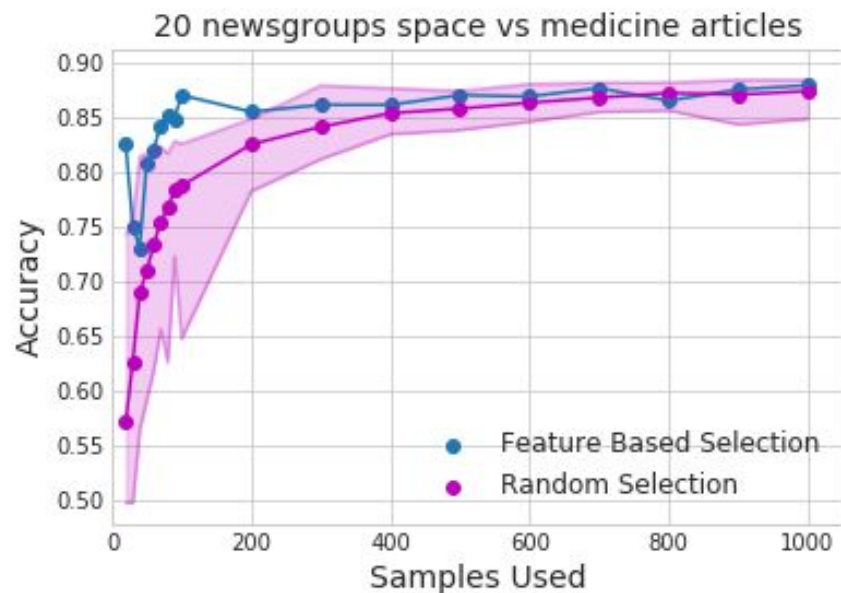


# Tutorials available on GitHub

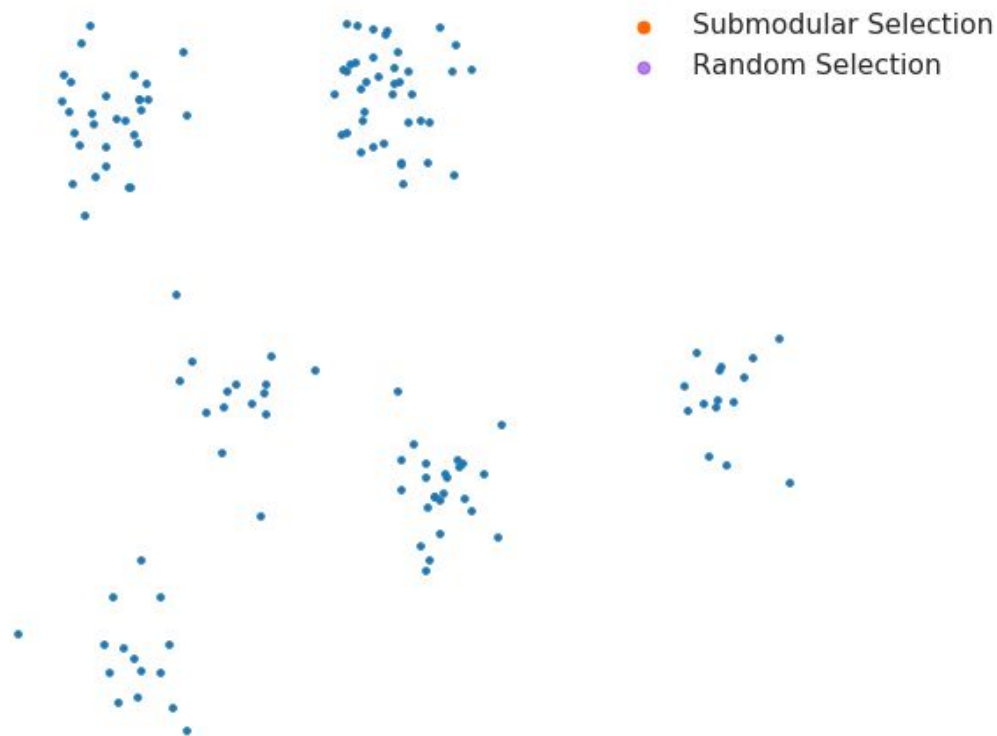
Branch: master ▾		pomegranate / tutorials /		Create new file	Upload files	Find file	History
 jmschrei ENH NB/BC notebook				Latest commit 5cd8d68 5 days ago			
..							
 old		ADD new overview tutorial		a month ago			
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<https://github.com/jmschrei/pomegranate/tree/master/tutorials>

# apricot implements submodular selection for training machine learning models faster



# apricot implements submodular selection for training machine learning models faster



# pomegranate

fast and flexible probabilistic modelling in python

Jacob Schreiber

Paul G. Allen School of Computer Science & Engineering  
University of Washington



jmschreiber91



@jmschrei



@jmschreiber91